

Table 2. *Interatomic distances for KNaThF₆*

3[Th-F(1)]*	2.28 (2) Å	3[K-F(1)]	2.68 (2) Å
3[Th-F(2)]	2.40 (2)	3[K-F(1)]	2.79 (2)
3[Th-F(2)]	2.42 (2)	3[K-F(2)]	2.87 (2)
3[Na-F(1)]	2.26 (2)	3[Na-F(2)]	2.54 (2)
F(1)-F(2)	2.72 (2)	2F(1)-F(1)	2.86 (3)
F(1)-F(2)	2.84 (2)	F(1)-F(2)	2.97 (2)

* The coefficient in front of the bond denotes the number of equal bonds in the structure.

Table 3. *Observed and calculated factors for KNaThF₆*

L	F _{obs}	F _{calc}	L	F _{obs}	F _{calc}	L	F _{obs}	F _{calc}	L	F _{obs}	F _{calc}	L	F _{obs}	F _{calc}	L	F _{obs}	F _{calc}	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	13	18	2	35	56	3	60	67	4	101	100	5	92	97	6	86	80	7
4	166	168	6	230	228	9	300	298	12	420	418	15	510	508	18	580	578	21
8	107	107	12	168	168	16	240	240	21	350	350	24	460	460	27	530	530	30
16	67	64	24	108	108	32	168	168	42	252	252	48	360	360	54	468	468	63
32	42	40	48	72	72	64	108	108	84	144	144	112	168	168	144	192	192	168
64	27	26	96	36	36	128	36	36	176	176	192	36	36	36	224	36	36	252
128	18	18	192	18	18	256	18	18	336	336	336	18	18	18	432	18	18	468
256	12	12	384	12	12	512	12	12	672	672	672	12	12	12	896	12	12	936
512	8	8	576	8	8	768	8	8	1008	1008	1008	8	8	8	1344	8	8	1380
1024	6	6	768	6	6	1024	6	6	1344	1344	1344	6	6	6	1792	6	6	1836
2048	4	4	1024	4	4	1344	4	4	1792	1792	1792	4	4	4	2352	4	4	2396
4096	3	3	1344	3	3	1792	3	3	2352	2352	2352	3	3	3	3072	3	3	3116
8192	2	2	1792	2	2	2352	2	2	3072	3072	3072	2	2	2	3984	2	2	4028
16384	1	1	2352	1	1	3072	1	1	3984	3984	3984	1	1	1	5088	1	1	5132
32768	0	0	3072	0	0	3984	0	0	5088	5088	5088	0	0	0	6544	0	0	6588
65536	0	0	3984	0	0	5088	0	0	6544	6544	6544	0	0	0	8392	0	0	8436
131072	0	0	5088	0	0	6544	0	0	8392	8392	8392	0	0	0	10688	0	0	10732
262144	0	0	6544	0	0	8392	0	0	10688	10688	10688	0	0	0	13408	0	0	13452
524288	0	0	8392	0	0	10688	0	0	13408	13408	13408	0	0	0	16896	0	0	16940
1048576	0	0	10688	0	0	13408	0	0	16896	16896	16896	0	0	0	21344	0	0	21388
2097152	0	0	13408	0	0	16896	0	0	21344	21344	21344	0	0	0	27040	0	0	27084
4194304	0	0	16896	0	0	21344	0	0	27040	27040	27040	0	0	0	34176	0	0	34220
8388608	0	0	21344	0	0	27040	0	0	34176	34176	34176	0	0	0	42944	0	0	42988
16777216	0	0	27040	0	0	34176	0	0	42944	42944	42944	0	0	0	53248	0	0	53292
33554432	0	0	34176	0	0	42944	0	0	53248	53248	53248	0	0	0	65984	0	0	66028
67108864	0	0	42944	0	0	53248	0	0	65984	65984	65984	0	0	0	82176	0	0	82220
124217728	0	0	53248	0	0	65984	0	0	82176	82176	82176	0	0	0	101824	0	0	101868
248435456	0	0	65984	0	0	82176	0	0	101824	101824	101824	0	0	0	124032	0	0	124076
496870912	0	0	82176	0	0	101824	0	0	124032	124032	124032	0	0	0	152640	0	0	152684
993741824	0	0	101824	0	0	124032	0	0	152640	152640	152640	0	0	0	187008	0	0	187052
1987483648	0	0	124032	0	0	152640	0	0	187008	187008	187008	0	0	0	228224	0	0	228268
3974967296	0	0	152640	0	0	187008	0	0	228224	228224	228224	0	0	0	280128	0	0	280172
7949934592	0	0	187008	0	0	228224	0	0	280128	280128	280128	0	0	0	342912	0	0	342956
14899869184	0	0	228224	0	0	280128	0	0	342912	342912	342912	0	0	0	416640	0	0	416684
29799738368	0	0	280128	0	0	342912	0	0	416640	416640	416640	0	0	0	500928	0	0	500972
59599476736	0	0	342912	0	0	416640	0	0	500928	500928	500928	0	0	0	600000	0	0	600044
119198953472	0	0	416640	0	0	500928	0	0	600000	600000	600000	0	0	0	722048	0	0	722092
238397906944	0	0	500928	0	0	600000	0	0	722048	722048	722048	0	0	0	859136	0	0	859180
476795813888	0	0	600000	0	0	722048	0	0	859136	859136	859136	0	0	0	1010240	0	0	1010284
953591627776	0	0	722048	0	0	859136	0	0	1010240	1010240	1010240	0	0	0	1180320	0	0	1180364
1907183255552	0	0	859136	0	0	1010240	0	0	1180320	1180320	1180320	0	0	0	1380480	0	0	1380524
3814366511104	0	0	1010240	0	0	1180320	0	0	1380480	1380480	1380480	0	0	0	1600640	0	0	1600684
7628733022208	0	0	1180320	0	0	1380480	0	0	1600640	1600640	1600640	0	0	0	1840800	0	0	1840844
15257466044416	0	0	1380480	0	0	1600640	0	0	1840800	1840800	1840800	0	0	0	2100960	0	0	2101004
30514932088832	0	0	1600640	0	0	1840800	0	0	2100960	2100960	2100960	0	0	0	2480160	0	0	2480204
61029864177664	0	0	1840800	0	0	2100960	0	0	2480160	2480160	2480160	0	0	0	2890240	0	0	2890284
122059728355328	0	0	2100960	0	0	2480160	0	0	2890240	2890240	2890240	0	0	0	3410320	0	0	3410364
244119456710656	0	0	2480160	0	0	2890240	0	0	3410320	3410320	3410320	0	0	0	4040400	0	0	4040444
488238913421312	0	0	2890240	0	0	3410320	0	0	4040400	4040400	4040400	0	0	0	4790480	0	0	4790524
976477826842624	0	0	3410320	0	0	4040400	0	0	4790480	4790480	4790480	0	0	0	5650560	0	0	5650604
1952955653685248	0	0	4040400	0	0	4790480	0	0	5650560	5650560	5650560	0	0	0	6630640	0	0	6630684
3905911307370496	0	0	4790480	0	0	5650560	0	0	6630640	6630640	6630640	0	0	0	7730720	0	0	7730764
7811822614740992	0	0	5650560	0	0	6630640	0	0	7730720	7730720	7730720	0	0	0	8940800	0	0	8940844
15623645289481984	0	0	6630640	0	0	7730720	0	0	8940800	8940800	8940800	0	0	0	10260880	0	0	10260924
31247290578963968	0	0	7730720	0	0	8940800	0	0	10260880	10260880	10260880	0	0	0	11700960	0	0	11701004
62494581157927936	0	0	8940800	0	0	10260880	0	0	11700960	11700960	11700960	0	0	0	13261040	0	0	13261084
124989162315855872	0	0	10260880	0	0	11700960	0	0	13261040	13261040	13261040	0	0	0	14941120	0	0	14941164
249978324631711744	0	0	11700960	0	0	13261040	0	0	14941120	14941120	14941120	0	0	0	16741200	0	0	16741244
499956649263423488	0	0	13261040	0	0	14941120	0	0	16741200	16741200	16741200	0	0	0	18661280	0	0	18661324
999913298526846976	0	0	14941120	0	0	16741200	0	0	18661280	18661280	18661280	0	0	0	20701360	0	0	20701404
1999826597053693952	0	0	16741200	0	0	18661280	0	0	20701360	20701360	20701360	0	0	0	22861440	0	0	22861484
3999653194107387904	0	0	18661280	0	0	20701360	0	0	22861440	22861440	22861440	0	0	0	25141520	0	0	25141564
7999306388214775808	0	0																

ther poorly resolved, this function yielded a discernible image of the molecule from which positional parameters for the remaining atoms could be assigned. A three-dimensional electron density map phased on these parameters clearly defined the atomic locations and yielded a trial structure essentially the same as that obtained from the superposition function. At this point a set of scaled structure factors was calculated for all 521 reflections. The reliability index was 0.44.

Refinement was carried out using the full-matrix least-squares program *ORFLS* (Busing, Martin & Levy, 1962).

The quantity minimized was $\sum w \left(F_o - \frac{1}{k} F_c \right)^2$. The *R* index

was lowered to a final value of 0.13 using individual isotropic temperature factors. The weighting scheme used was

$$w = 1/|F| \text{ for } |F| > 4|F|_{\min},$$

$$w = \frac{1}{4|F|_{\min}} \text{ for } |F| \leq 4|F|_{\min}.$$

All unobserved reflections were assigned zero weight. Hydrogen atom parameters were not included in the refinement. Final atomic parameters and estimated standard deviations are listed in Table 1. A list of observed and calculated structure factors is available from the authors on request. The rather large thermal parameters are probably a reflection of the fact that this compound is highly sensitive to X-radiation. During data collection several crystals had to be employed and all were observed to rapidly discolor in the X-ray beam. Because of these experimental difficulties, further refinement of the data, including anisotropic ther-

Table 1. Final atomic parameters

E.s.d.'s are given in parentheses.

	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i>
S	0.7664 (10)	0.7850 (6)	0.0496 (6)	5.63 (11)
O(1)	0.8264 (30)	0.6978 (17)	-0.0586 (20)	9.35 (45)
O(2)	0.7278 (27)	0.9223 (17)	-0.0073 (17)	8.28 (41)
O(3)	0.8742 (27)	0.7818 (16)	0.1827 (18)	8.08 (38)
C(1)	0.5776 (35)	0.7163 (21)	0.0856 (22)	5.68 (46)
C(2)	0.4235 (35)	0.7745 (21)	0.0300 (22)	5.37 (44)
C(3)	0.2706 (37)	0.7290 (21)	0.0576 (24)	5.90 (46)
C(4)	0.2787 (39)	0.6096 (23)	0.1467 (24)	6.29 (50)
C(5)	0.4332 (36)	0.5445 (20)	0.2074 (23)	5.66 (48)
C(6)	0.5788 (38)	0.5993 (22)	0.1767 (24)	6.00 (48)
N(1)	0.1321 (34)	0.5537 (19)	0.1810 (21)	6.97 (45)
N(2)	0.0122 (36)	0.5099 (22)	0.2119 (23)	8.68 (54)

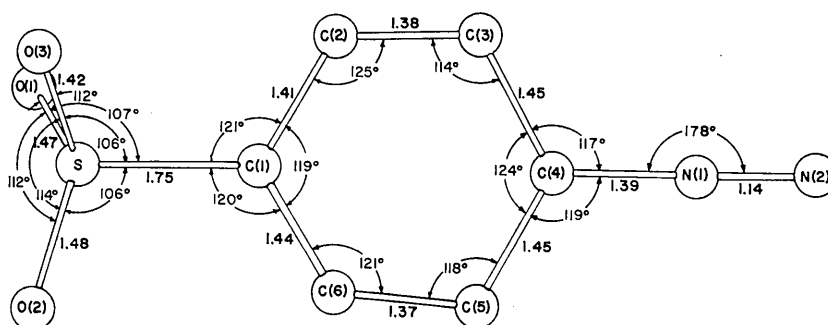


Fig. 1. Bond lengths and angles in the molecule.

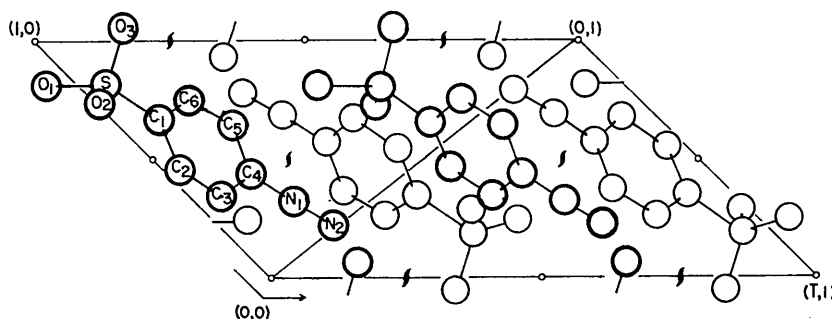


Fig. 2. Projection of the structure down the *b* axis.

mal analysis and determination of hydrogen atom parameters, seemed unwarranted.

Bond lengths and angles calculated from the final atomic parameters are shown in Fig. 1. A view of the crystal structure projected down the b axis is shown in Fig. 2. Excluding the oxygen atoms, the molecule is planar within experimental error. The equation of the least-squares plane through the phenyl ring is $-0.4583x + 5.2702y + 7.3449z = 4.1023$. The dimensions of the sulfonate group are similar to those found in a variety of related compounds.

The observed dimensions of the ring suggest that the molecule is quinoid in character. Of interest are the dimensions of the diazonium group as compared with those observed in structures of the type $(\text{ArN}_2)^+(\text{X})^-$. The C(4)–N(1) distance of 1.39 Å compares with the corresponding bond length of 1.385 Å found in phenyldiazonium chloride (Rømming, 1963) and 1.41 Å in phenyldiazonium tribromide (Anderson & Rømming, 1962); it appears to be significantly shorter than the value of 1.45 Å reported for the double salt of ferric chloride and *o*-methylphenyldiazonium chloride (Polynova, Bokii & Porai-Koshits, 1965). The N(1)–N(2) bond length of 1.14 Å is marginally longer than the values of 1.097, 1.11 and 1.11 Å respectively re-

ported for these salts. The diazonium group is linear within experimental error.

The molecular packing is quite reasonable with no intermolecular distances shorter than the sum of the normally accepted van der Waals radii. The shortest intermolecular approaches are found at the polar ends of the molecule. These are 2.92 Å between N(2) and O(3) $(-1+x, y, z)$; 2.92 Å between N(2) and O(1) $(1-x, 1-y, \bar{z})$; and 2.79 Å between N(1) and O(1) $(1-x, 1-y, \bar{z})$.

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Acta Cryst. (1970). **B26**, 1189

Bond lengths and thermal parameters of potassium metaborate, $\text{K}_3\text{B}_3\text{O}_6$. By W. SCHNEIDER* and G. B. CARPENTER, Metcalf Chemical Laboratories, Brown University, Providence, Rhode Island 02912, U.S.A.

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The results of a refinement of the structure of $\text{K}_3\text{B}_3\text{O}_6$ are described. The space group is $R\bar{3}c$ and the hexagonal axes are $a=12.76$ and $c=7.34$ Å. In the cyclic $\text{B}_3\text{O}_6^{3-}$ ion the endocyclic B–O distances are 1.398 Å and the exocyclic B–O distances are 1.331 Å. The results agree closely with the original results of Zachariassen (1937). The dimensions of the ion cannot be reconciled with the distances found in the isostructural $\text{Na}_3\text{B}_3\text{O}_6$ on the basis of a simple correlation between bond strength and bond length.

The cyclic metaborate ion $\text{B}_3\text{O}_6^{3-}$ was discovered by Zachariassen (1937) in potassium metaborate. This ion consists of a planar six-membered ring of alternating boron and oxygen atoms with B–O = 1.38 Å, and three other oxygen atoms bonded to the boron atoms at B–O = 1.33 Å. The same ion was found also in sodium metaborate (Fang, 1938).

A later nuclear magnetic resonance study (Bray, Edwards, O'Keefe, Ross & Tatsuzaki, 1961) of potassium metaborate suggested that boron might not have the trigonal coordination reported from the original diffraction work.

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At that time the present authors undertook a re-examination of the potassium compound in order to resolve the discrepancy. We found that Zachariassen's model was in fact quite accurate, giving an R value of 12% with our $0kl$ data.

Subsequently Marezio, Plettinger & Zachariassen (1963*b*) redetermined the structure of the isostructural compound $\text{Na}_3\text{B}_3\text{O}_6$, and found B–O = 1.433 in the ring and B–O = 1.280 Å outside the ring. This is the extreme difference found for bonds to trigonal boron. The corresponding two points are the ones that lie farthest off the calculated bond order – bond length curve of Coulson & Dingle (1968). Since we did not find such a large difference in B–O distances in the potassium compound, it seems worthwhile now to report our results.

Table 1. *Parameters for $\text{K}_3\text{B}_3\text{O}_6$*

	x	β_{11}	$\beta_{22} = \beta_{12}$	β_{33}	$\beta_{13} = \beta_{23}$
K	0.5613 (1)	0.0025 (1)	0.0021 (1)	0.0051 (2)	0.0006 (1)
B	0.8889 (6)	0.0024 (3)	0.0034 (5)	0.0040 (9)	–0.0008 (4)
O(1)	0.7843 (3)	0.0024 (2)	0.0025 (3)	0.0064 (7)	–0.0007 (3)
O(2)	0.1084 (4)	0.0018 (2)	0.0015 (3)	0.0113 (8)	–0.0002 (4)

Standard deviations in the last digit are given in parentheses.